

Impedance, Resonance, and Filters



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VO1NO

A Quick Review...

- Before discussing Impedance, we must first understand capacitive and inductive reactance.

Reactance

- **Reactance is the opposition to the flow of Alternating Current (AC).**
- **Reactance has no effect on the flow of Direct Current (DC).**

Capacitive Reactance

- **Capacitive Reactance** is the **opposition** to the **flow of AC** by capacitance.
- As the **frequency of the AC** increases, **Capacitive Reactance** decreases.
- The **Symbol for Capacitive Reactance** is X_C .
- X_C is expressed in **ohms**.
- Even though it is expressed in ohms, **power is not dissipated by Reactance!** Energy stored in a capacitor during **one part of the AC cycle** is simply returned to the circuit during the **next part of the cycle!**

Capacitive Reactance

$$X_C = \frac{1}{2 \pi f C}$$

- Where:
F = frequency in Hertz
C = capacitance in Farads
 $\pi = 3.14$

Inductive Reactance

- **Inductive Reactance** is the **opposition** to the **flow of current** in an **AC circuit** caused by an **inductor**.
- As the **frequency increases**, Inductive Reactance **also increases**.
- The **symbol for Inductive Reactance** is X_L .
- Even though it is expressed in ohms, **power is not dissipated by Reactance!** Energy stored in an **inductor's magnetic field** during **one part of the AC cycle** is simply **returned to the circuit** during the **next part of the cycle!**

Inductive Reactance

$$X_L = 2 \pi f L$$

- Where:

f = frequency in Hertz

L = inductance in henrys

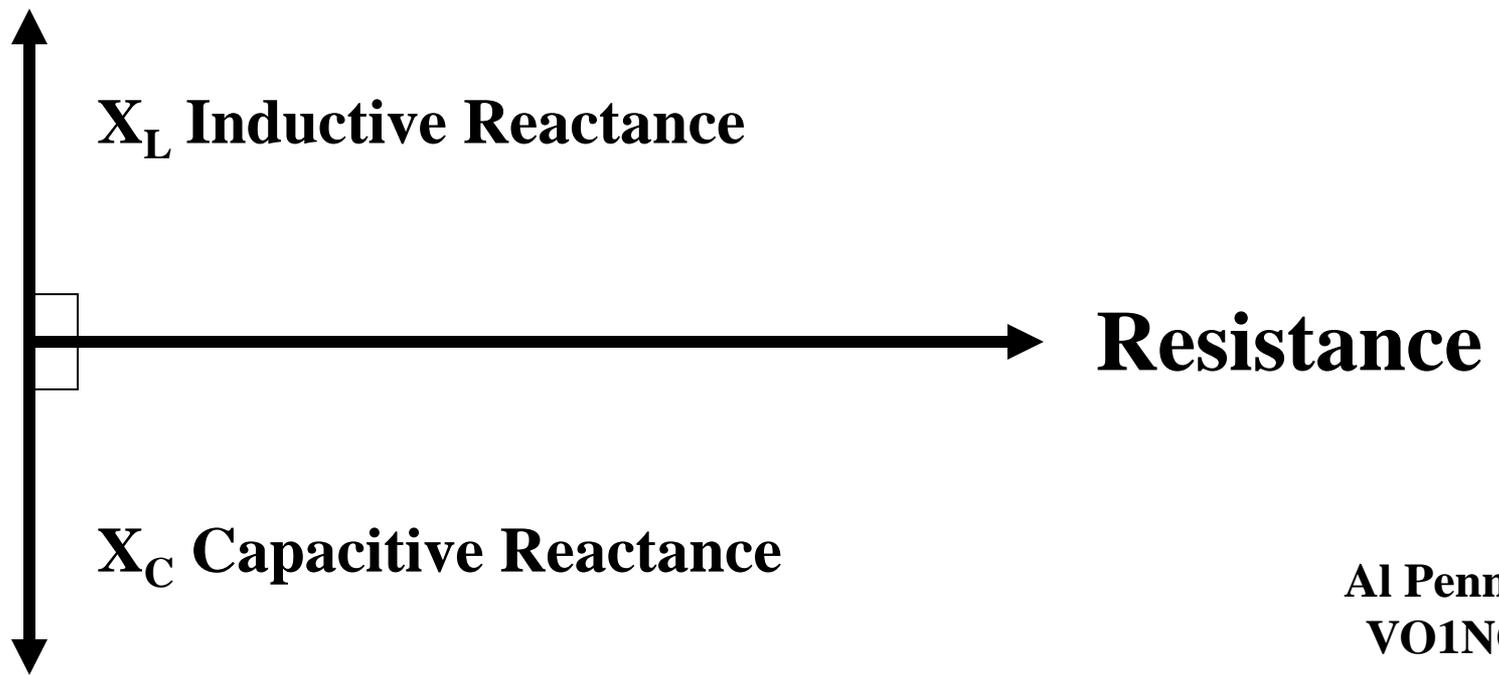
$\pi = 3.14$

Current versus Voltage

- In a simple **resistive** circuit, the **current and voltage are always in phase.**
- For reasons beyond the scope of the Basic Course, the current and voltage are **not in phase in AC circuits** that contain **capacitance and/or inductance.**
- The **current** across a **capacitor** leads the voltage by **90 degrees.**
- The **current** across an **inductor** lags the voltage by **90 degrees.**

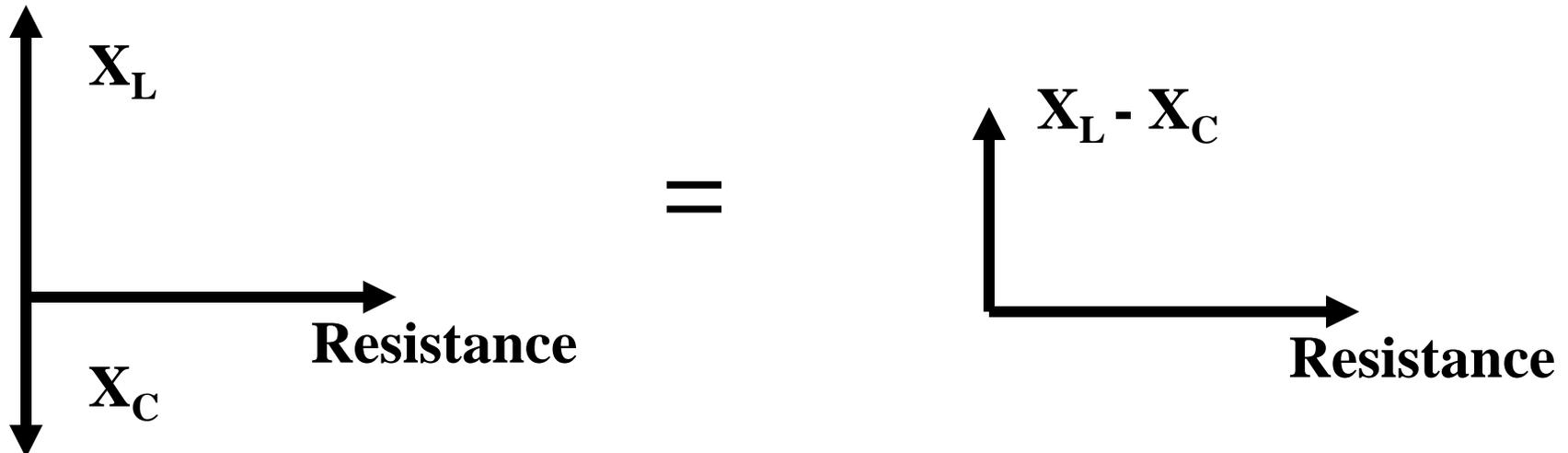
Vector Representation

- When plotted as **vectors**, **series circuits** containing Inductance, Capacitance and Resistance (**LCR**) can be represented as such:



Inductive vs Capacitive Reactance

- Inductive and Capacitive Reactance **cannot** be **added together** to give an overall reactance.
- In fact, they tend to **cancel each other out**.

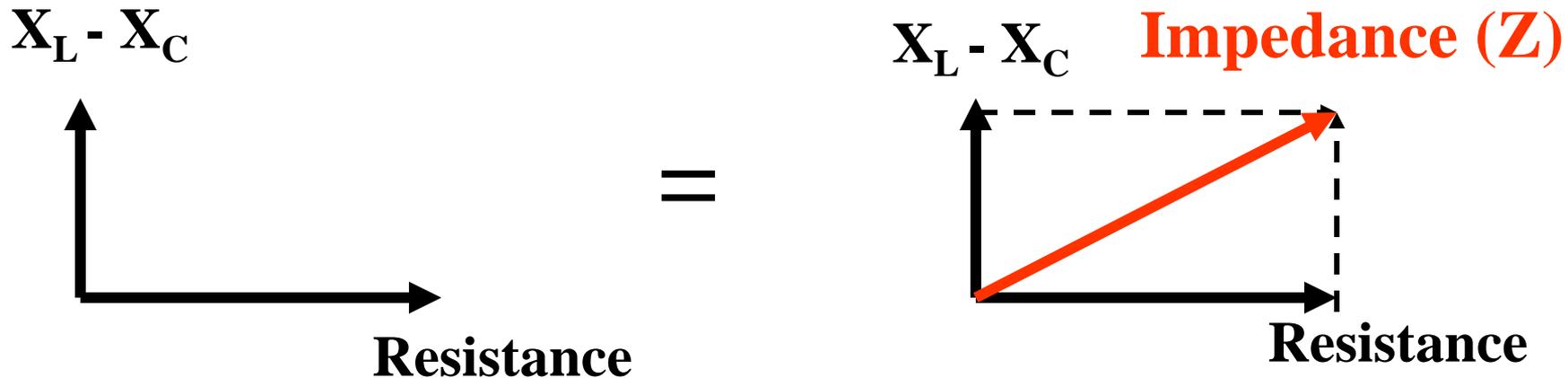


Impedance

- When a circuit contains both **resistance** and **reactance**, the **opposition to the flow of AC** is called **Impedance**, abbreviated **Z**.
- Because **Resistance** and **Reactance** are **not in phase** however, we must use **vectors** to determine the **Impedance**, even if Inductive and Capacitive Reactance have partly **cancelled each other out**.

Vector Addition

Through the use of **vector addition**, the Impedance can be determined...



LCR Circuit Impedance Formula

- Rather than plot vectors every time we need to determine impedance however, we can use a **formula**:

$$\mathbf{Z} = \sqrt{\mathbf{R}^2 + (\mathbf{X}_L - \mathbf{X}_C)^2}$$

- Note that because the difference between \mathbf{X}_L and \mathbf{X}_C is squared, **it doesn't matter** what term is subtracted from what – you can use $\mathbf{X}_C - \mathbf{X}_L$ if that is more convenient.

LCR Circuit Impedance Example

- Resistance = 120 Ohms
- $X_L = 40$ Ohms
- $X_C = 130$ Ohms

- $Z = \text{Sqr Root} [R^2 + (X_C - X_L)^2]$

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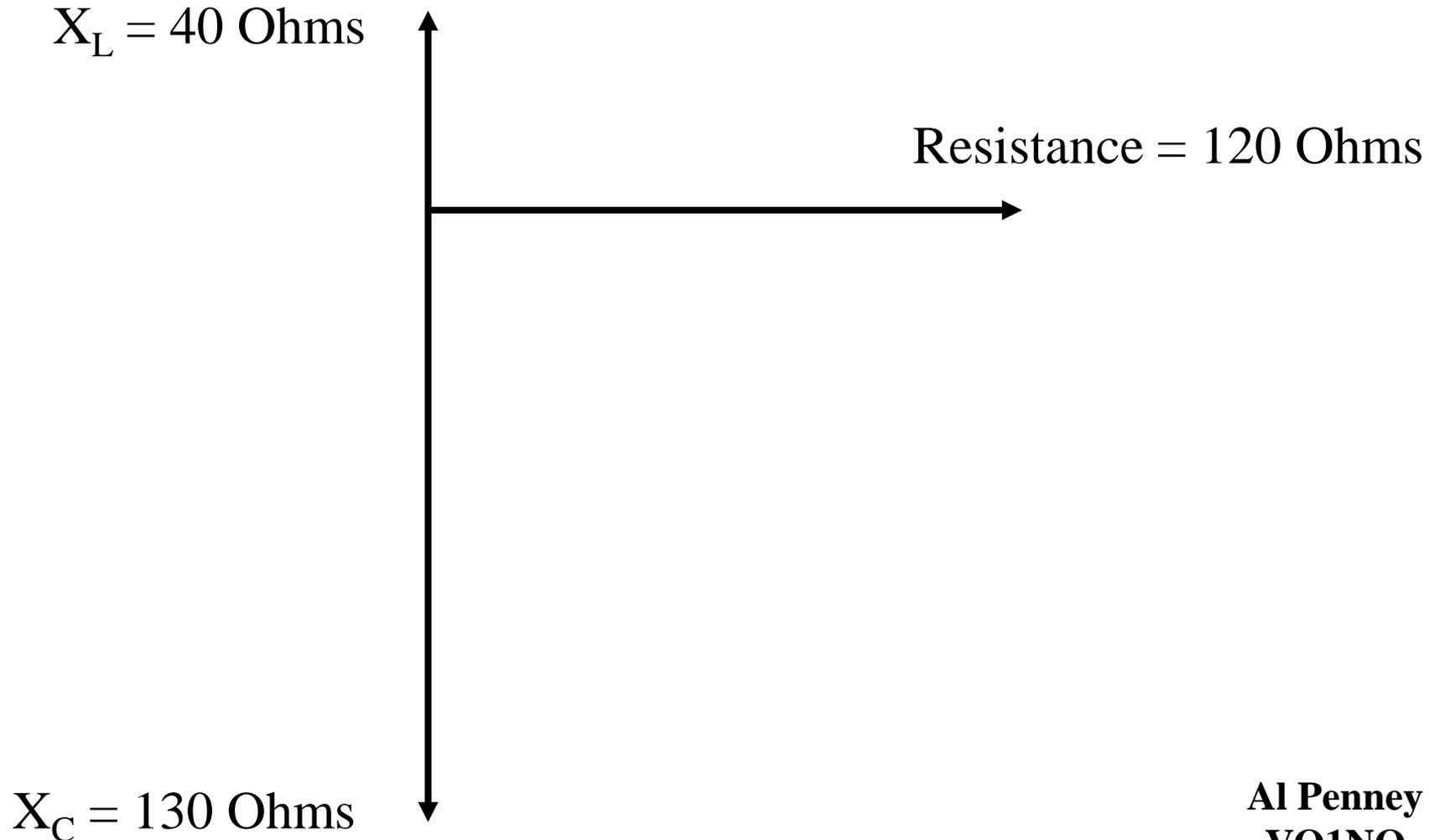
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LCR Circuit Impedance Example

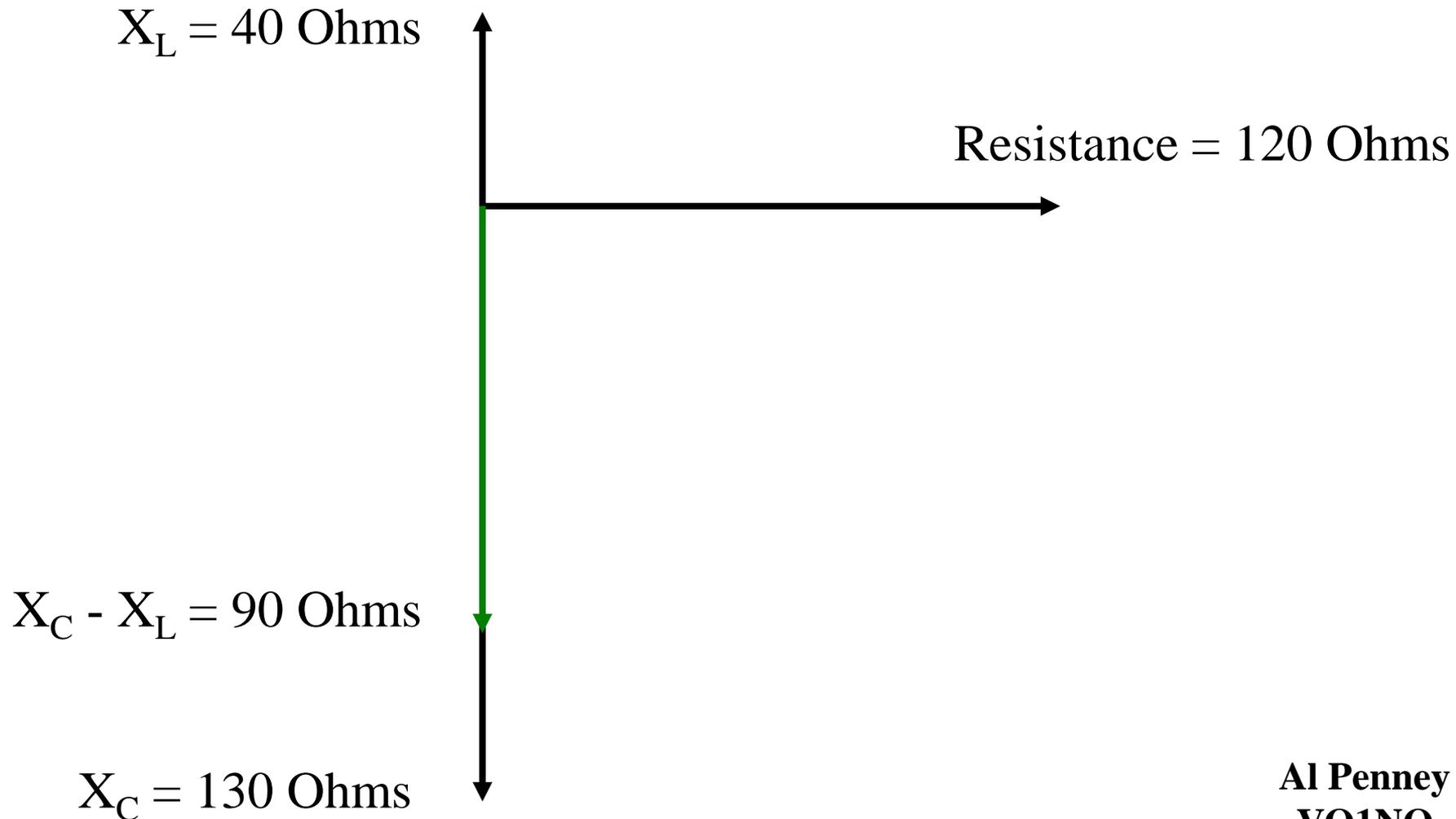
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= 150 Ohms

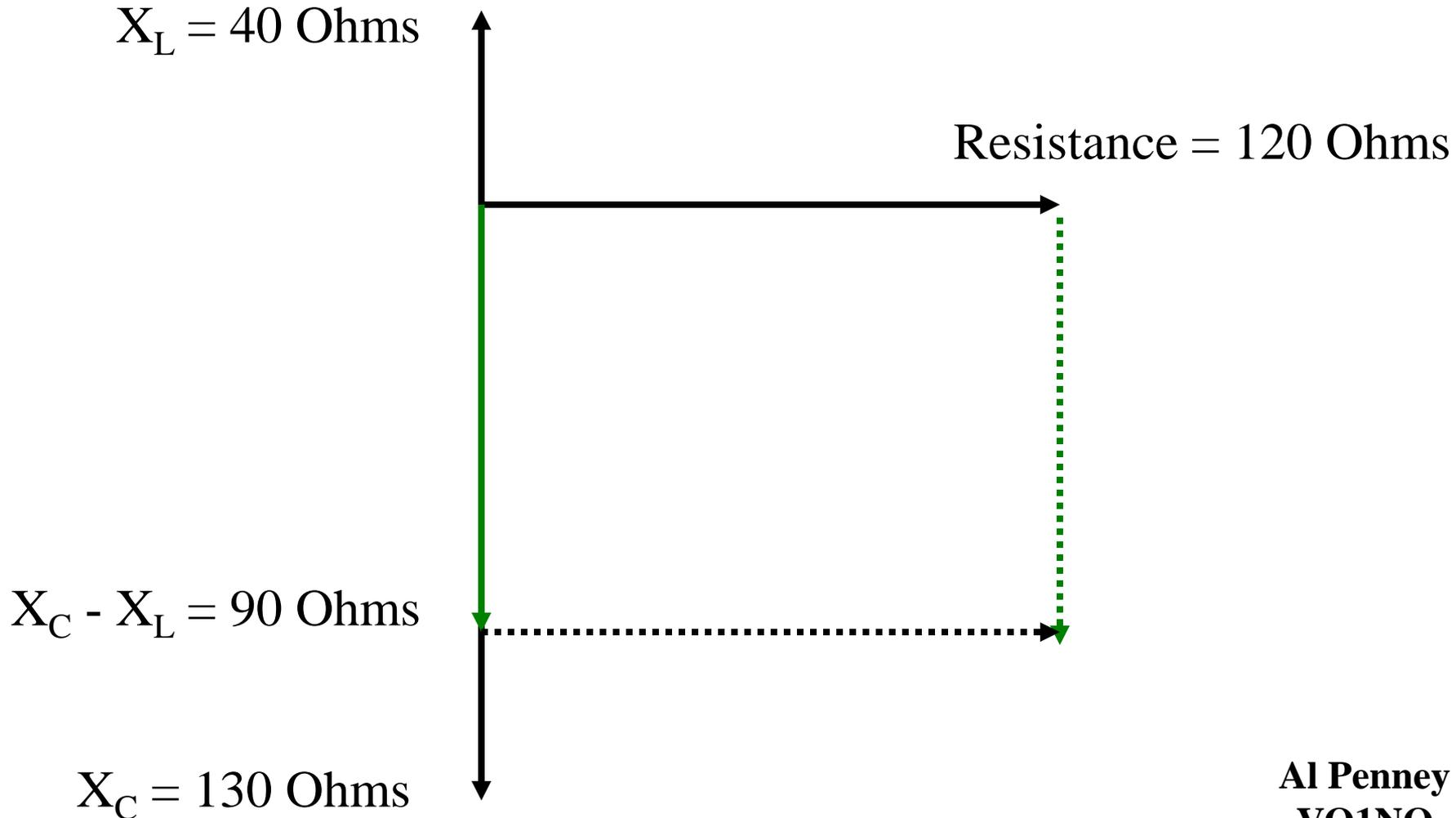
LCR Circuit Impedance Example



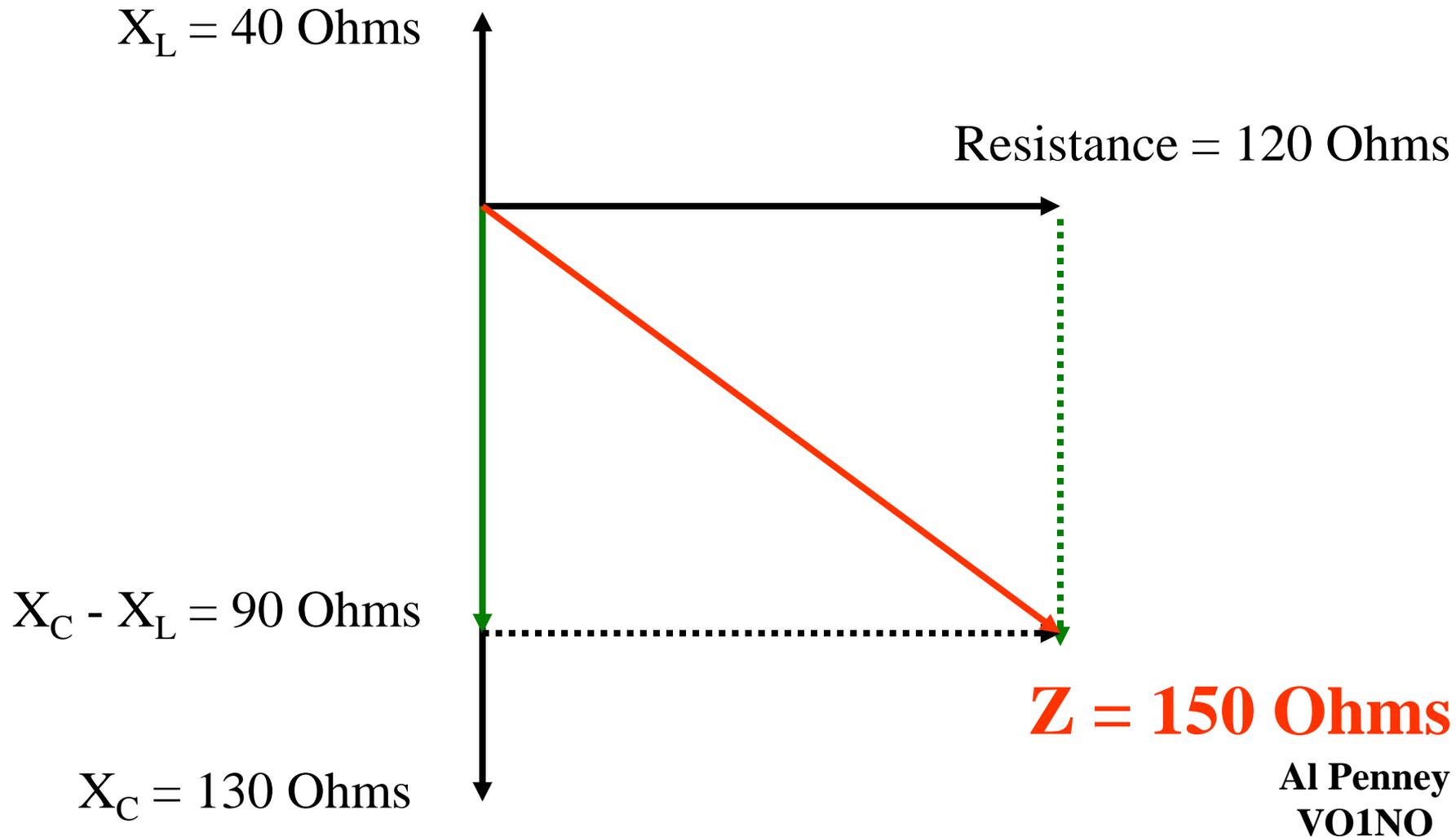
LCR Circuit Impedance Example



LCR Circuit Impedance Example



LCR Circuit Impedance Example



Impedance Matching

- Many electronic devices and circuits (speakers, microphones, antennas, transmission lines, amplifiers etc.) have their own **characteristic impedance**.
- When interconnecting these devices and circuits, **maximum power transfer** will take place if the various **impedances are matched**.

Matching with Transformers

- **Transformers** are often used to **match impedances** which are primarily **resistive**.
- This is especially true for **antenna and transmission line systems**.
- Take the matching transformer (**Balun – BALanced to UNbalanced**) used to match 300 Ohms to 75 Ohms in TV systems.

300 – 75 Ohm Balun

- These **matching transformers** are widely used for TV systems, and consist of a **small ferrite core** with **two windings**.
- In addition to the **impedance transformation**, it also converts between a **balanced** system and an **unbalanced** system.



Number of Turns

- Different impedances can be matched quite easily by adjusting the number of turns using the following formula:

$$\mathbf{Z_S / Z_P = N_S^2 / N_P^2}$$

Or...

$$\mathbf{N_S / N_P = \sqrt{Z_S / Z_P}}$$

Number of Turns - Example

- $Z_S = 300$ Ohms, $Z_P = 75$ Ohms

$$N_S / N_P = \sqrt{Z_S / Z_P}$$

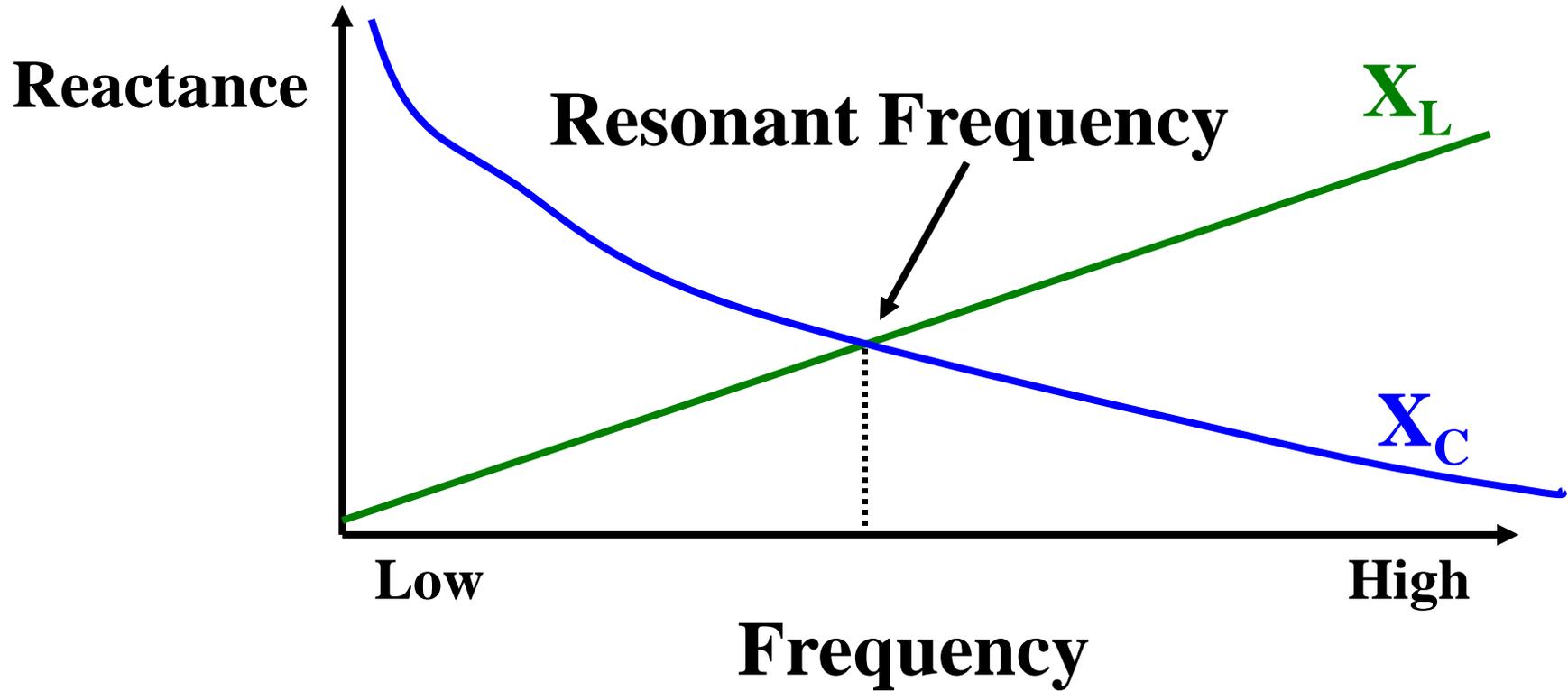
$$N_S / N_P = \sqrt{300 / 75} = \sqrt{4} = 2$$

- The **turns ratio** is 2:1 ie: for **every turn** on the **primary** winding, there are **two** on the **secondary** winding.
- The actual number of turns depends on the core material.

Resonance

- In electronic circuits, a special condition exists when **Inductive** and **Capacitive Reactance** are **equal** to each other ($X_L = X_C$).
- When that happens in Series LCR circuits, X_L and X_C **cancel** each other out, leaving only Resistance to oppose the flow of AC current.
- This condition is known as **Resonance**, and occurs at **only one frequency**, known as the **Resonant Frequency** (F_R).

Resonant Frequency



Resonant Frequency

- At Resonance, $X_C = X_L$ so

$$X_C = \frac{1}{2\pi f C} = X_L = 2\pi f L$$

- With a little mathematical wizardry, we can rearrange that equation to determine the **Resonant Frequency F_R** as follows...

Resonant Frequency

$$F_R = \frac{1}{2\pi\sqrt{LC}}$$

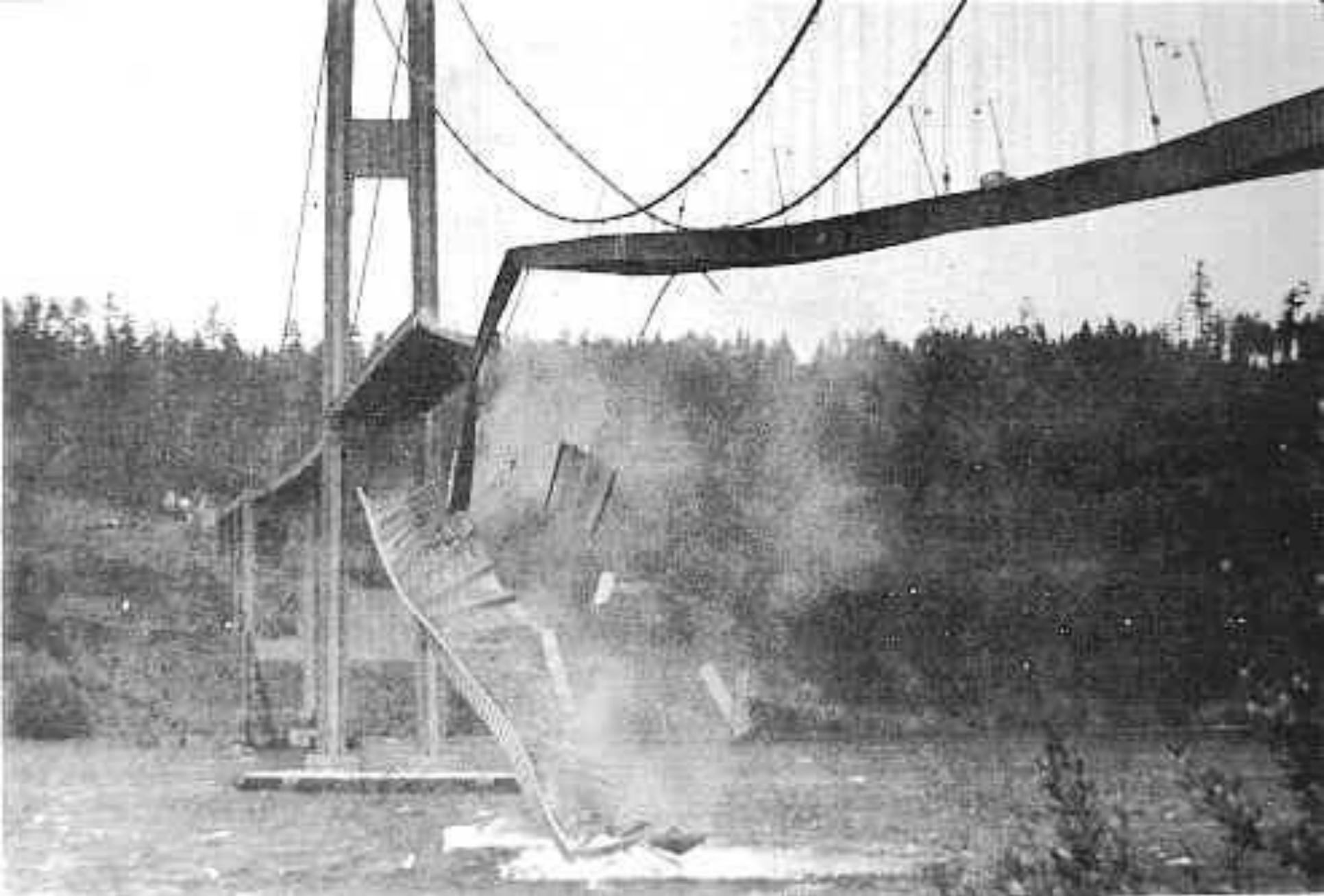
- Where:

F_R = Resonant Frequency in Hertz

L = Inductance in henrys

C = Capacitance in Farads

**Resonance is not always a good
thing however...**



Tacoma Narrows suspension bridge

Al Penney
V01NO

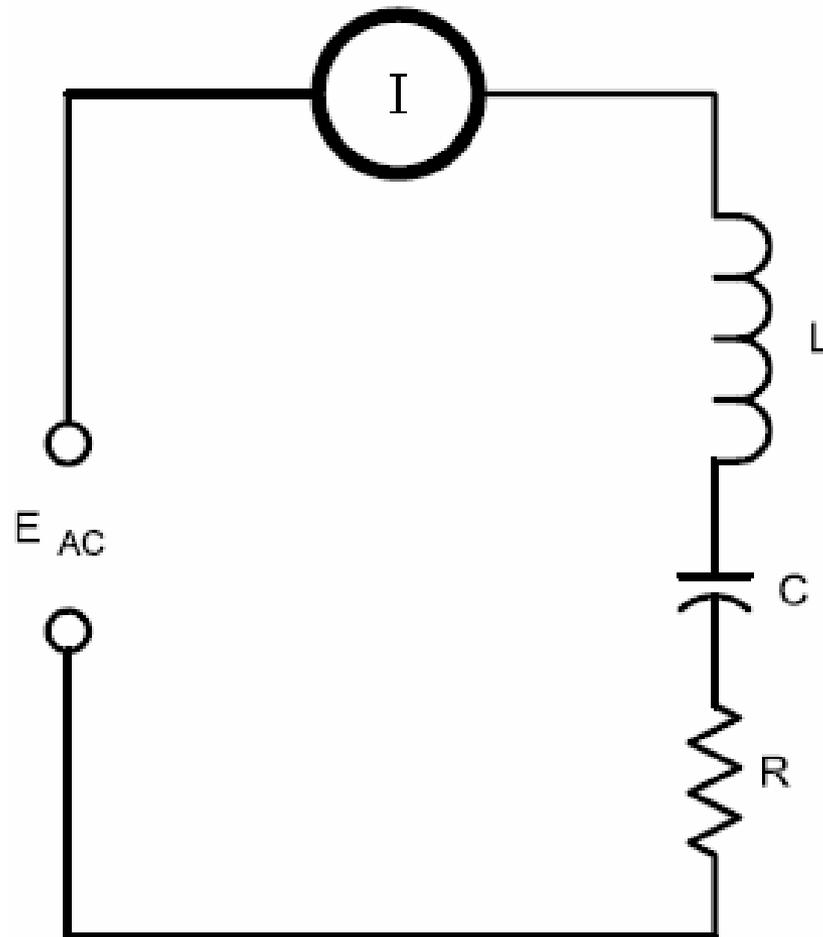
Tuned Circuits

- Circuits containing **Capacitors and Inductors** are often referred to as **Tuned Circuits**.
- They have **many uses** in electronics – every time you tune a radio, you are varying the **resonant frequency** of a **tuned circuit**.

Series LCR Circuit

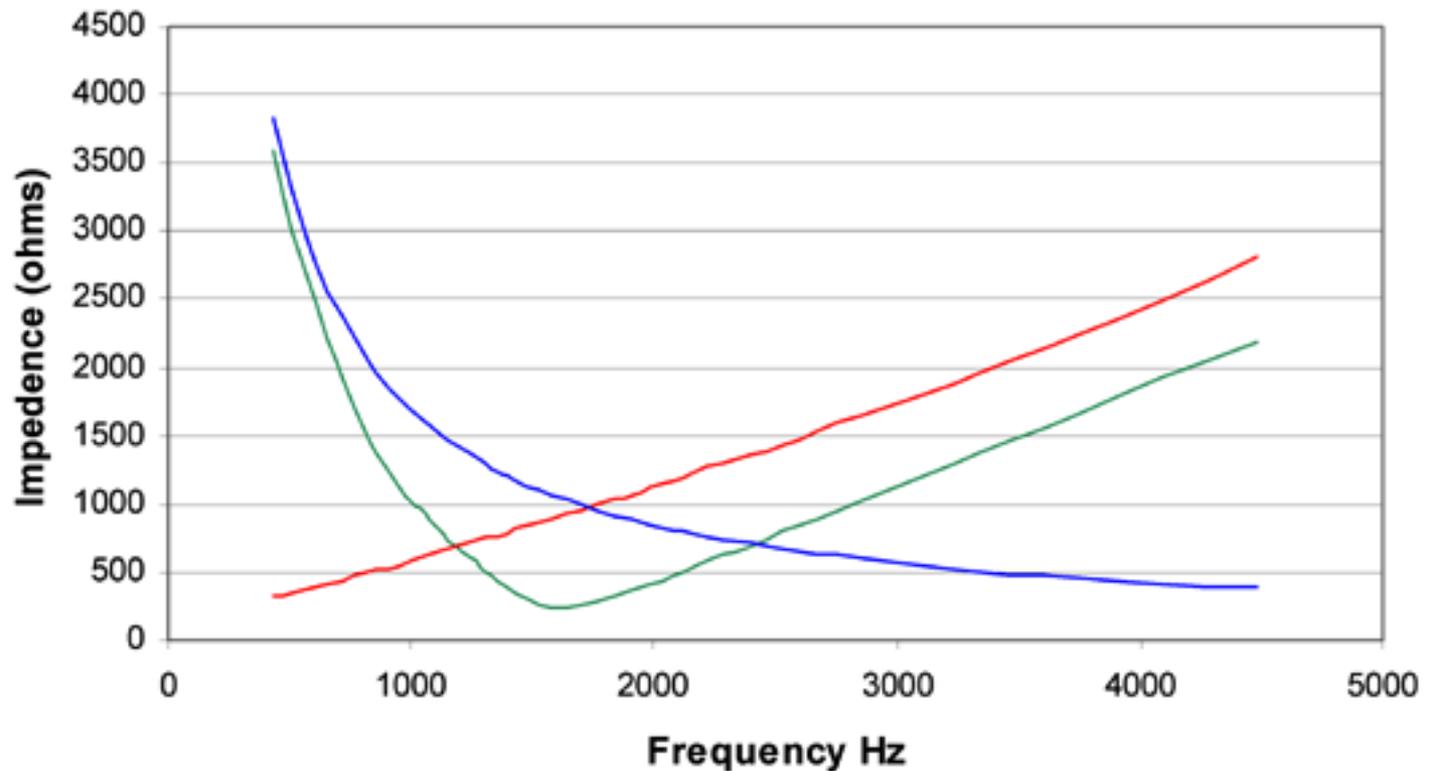
- When a **Series LCR** circuit is in **Resonance**, **current** in that circuit is at its **greatest** (the **Impedance** is at its **lowest**).
- There are **two ways** to achieve **Resonance** in **Series LCR** circuits:
 - **Vary the applied frequency** until we find the point where $X_C = X_L$.
 - Keep the frequency constant and **vary the value of the capacitance or inductance**, or both, until $X_C = X_L$.

Series LCR Circuit



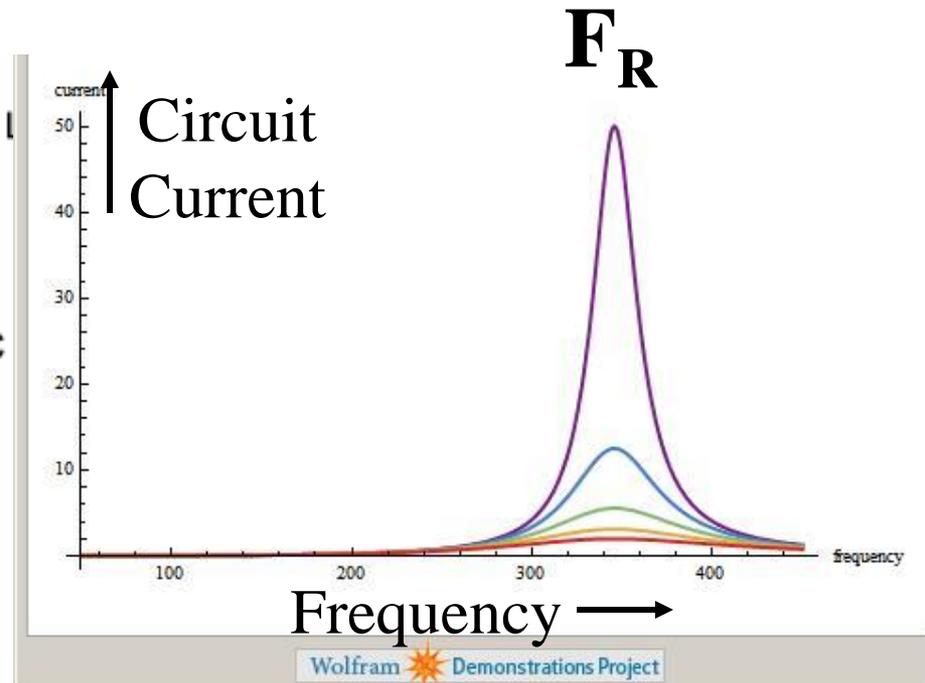
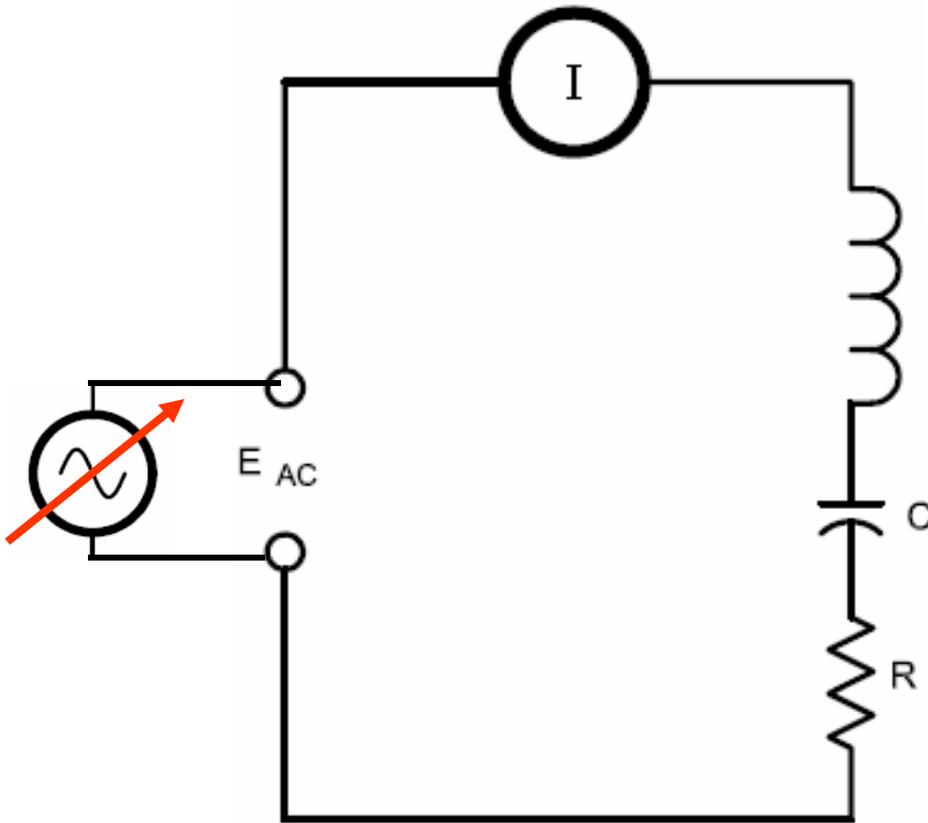
Series LCR Circuit Impedance

L/C in Series .1H/.1uF

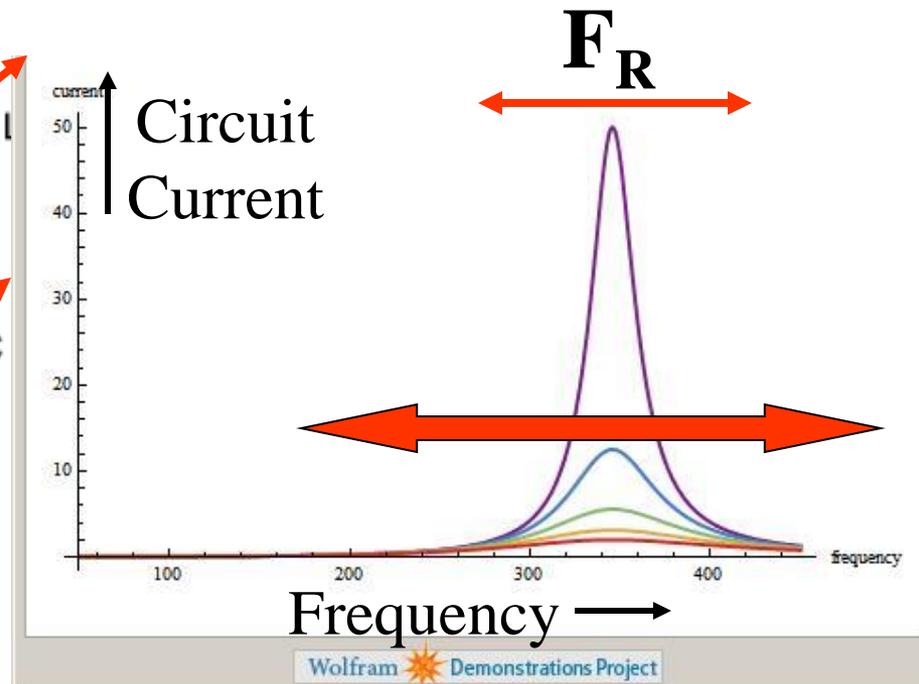
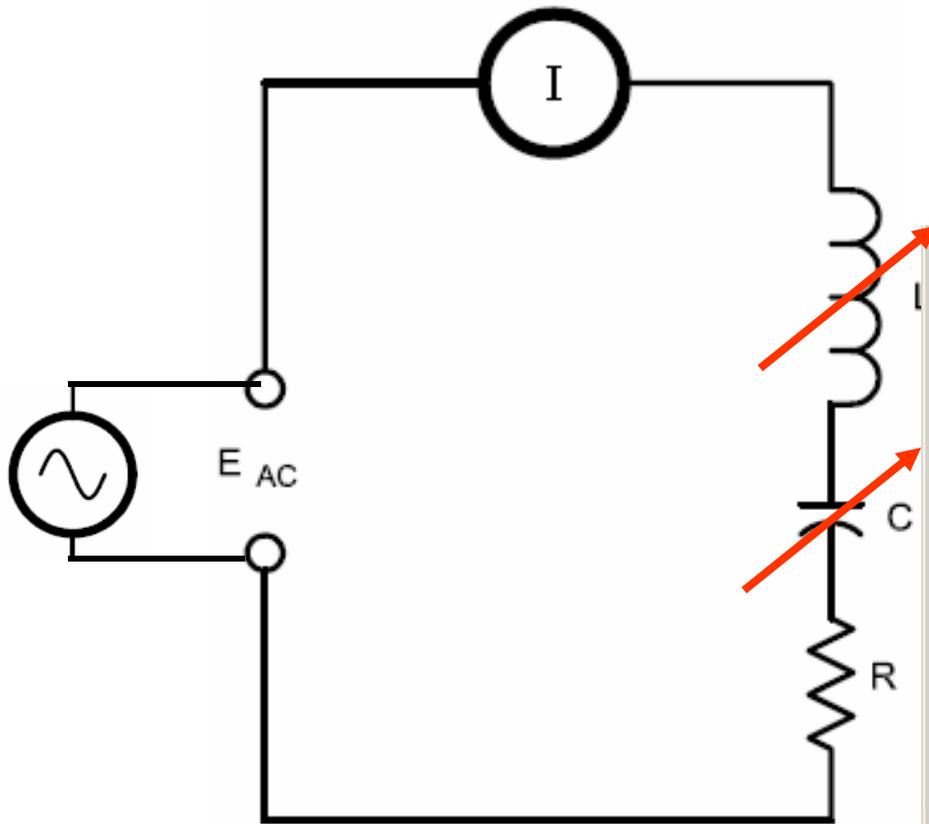


Series .1H Inductor .1uF Cap

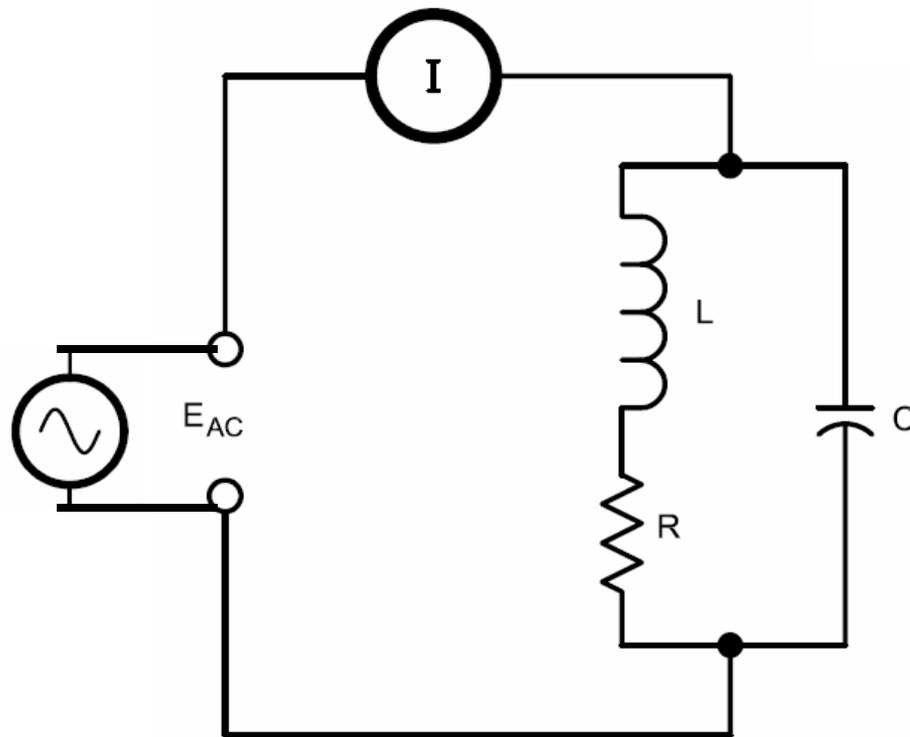
Varying the Frequency



Varying Capacitance or Inductance



Parallel LCR Circuits

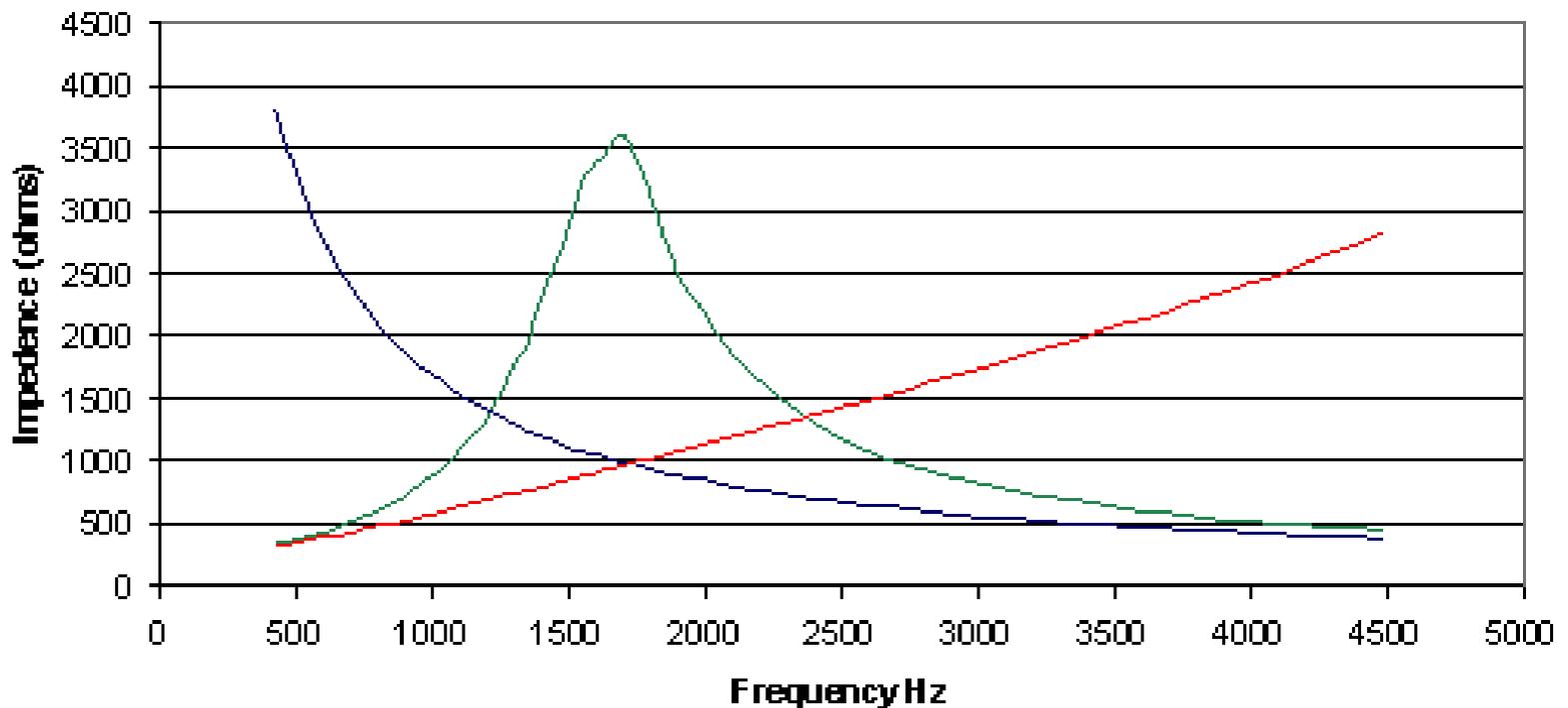


Parallel LCR Circuits

- In a **Parallel LCR Circuit**, the **current** is **lowest at Resonance** (the **impedance** is at its **highest**).
- Parallel LCR circuits are used to **reject a specific frequency** while allowing all others to pass.

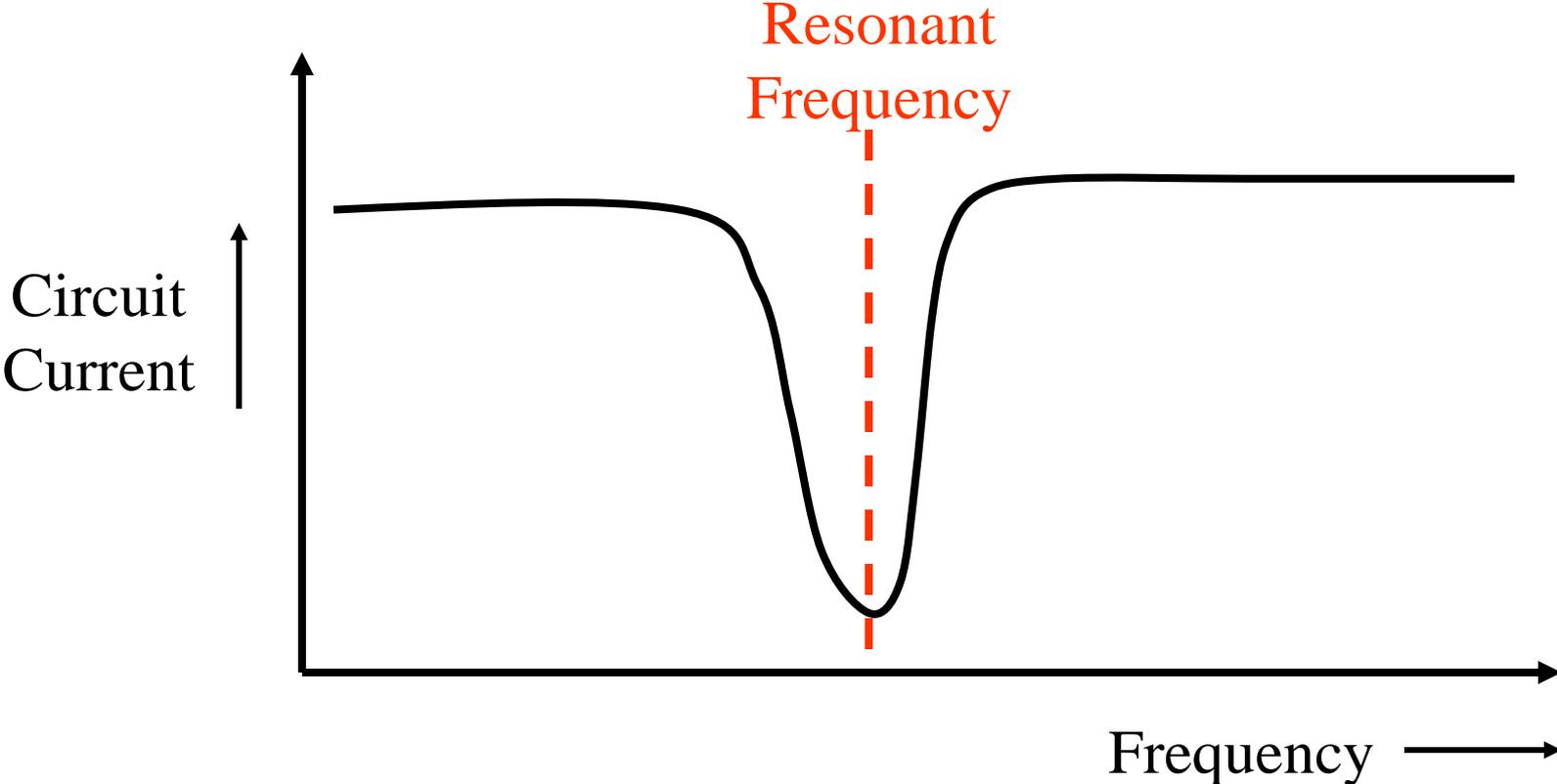
Parallel LCR Circuit Impedance

L/C in Parallel .1H/.1uF



Parallel .1uF Cap .1H Inductor

Parallel LCR Circuit Current

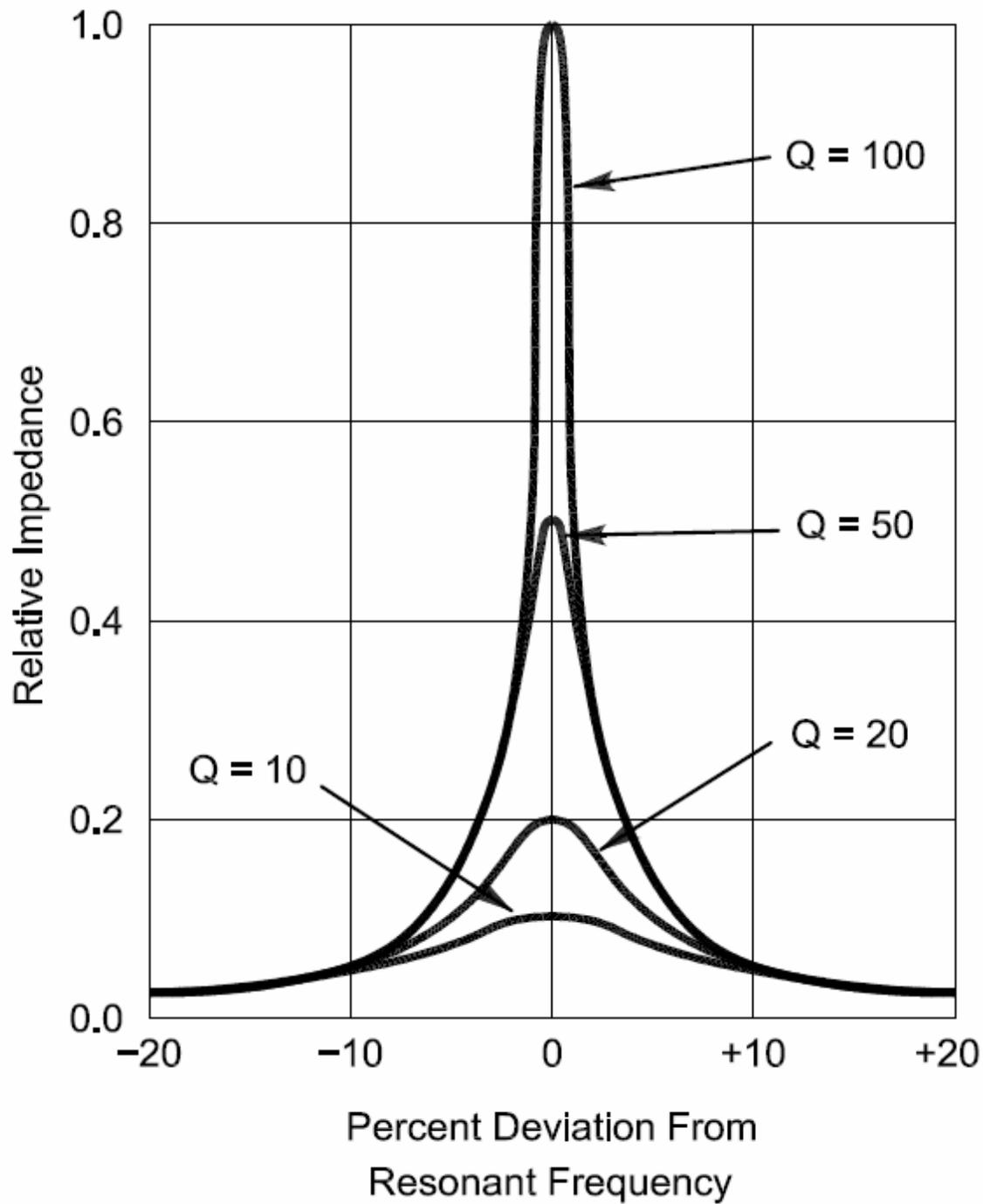


Circuit Quality

- In a **resonant series LCR circuit**, energy is stored **alternately** in the **electric field of the capacitor**, and then the **magnetic field of the inductor**.
- This causes a **current** to flow **between them**.
- Anything that **removes energy** from this circuit **broadens the range of frequencies** affected by the circuit, but **increases the impedance** at the **resonant frequency**.

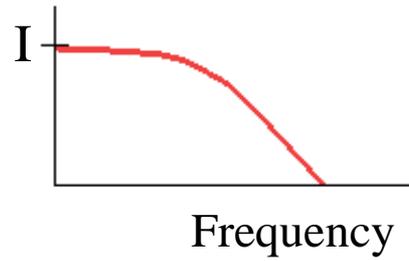
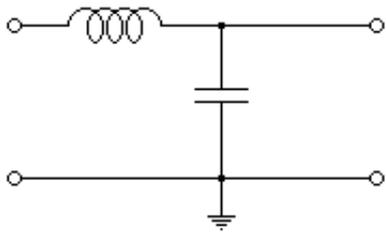
Circuit Quality

- The “**Q**”, or **Quality** of a series LCR circuit is defined as the **ratio** of either X_C or X_L to the **resistance** in the circuit.
- **Below** resonance “**Q**” = X_C / R
- **Above** resonance “**Q**” = X_L / R
- At resonance $X_C = X_L$
- A “**Q**” of **100** is **high**, while a “**Q**” of **10** is **low**.

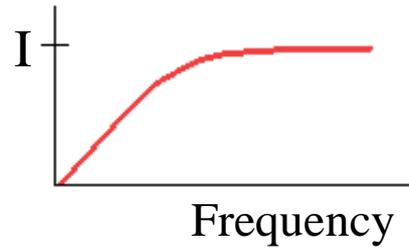
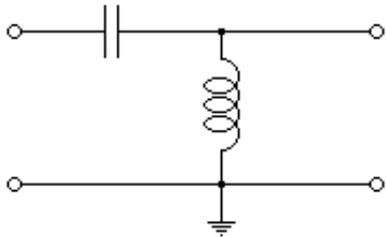


Filters

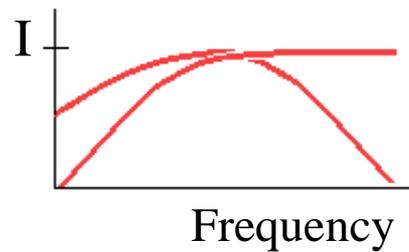
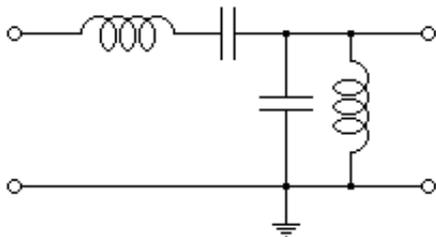
- By the proper selection of capacitors and inductors, it is possible to design **Filters** that can **pass desired frequencies**, and **reject unwanted frequencies**.



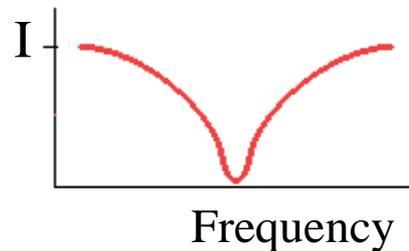
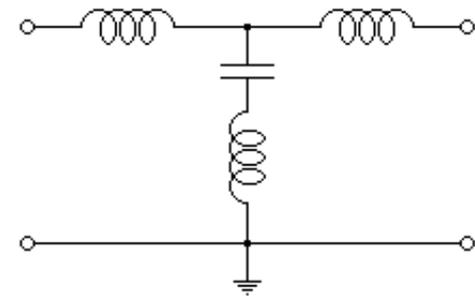
Low Pass Filter



High Pass Filter

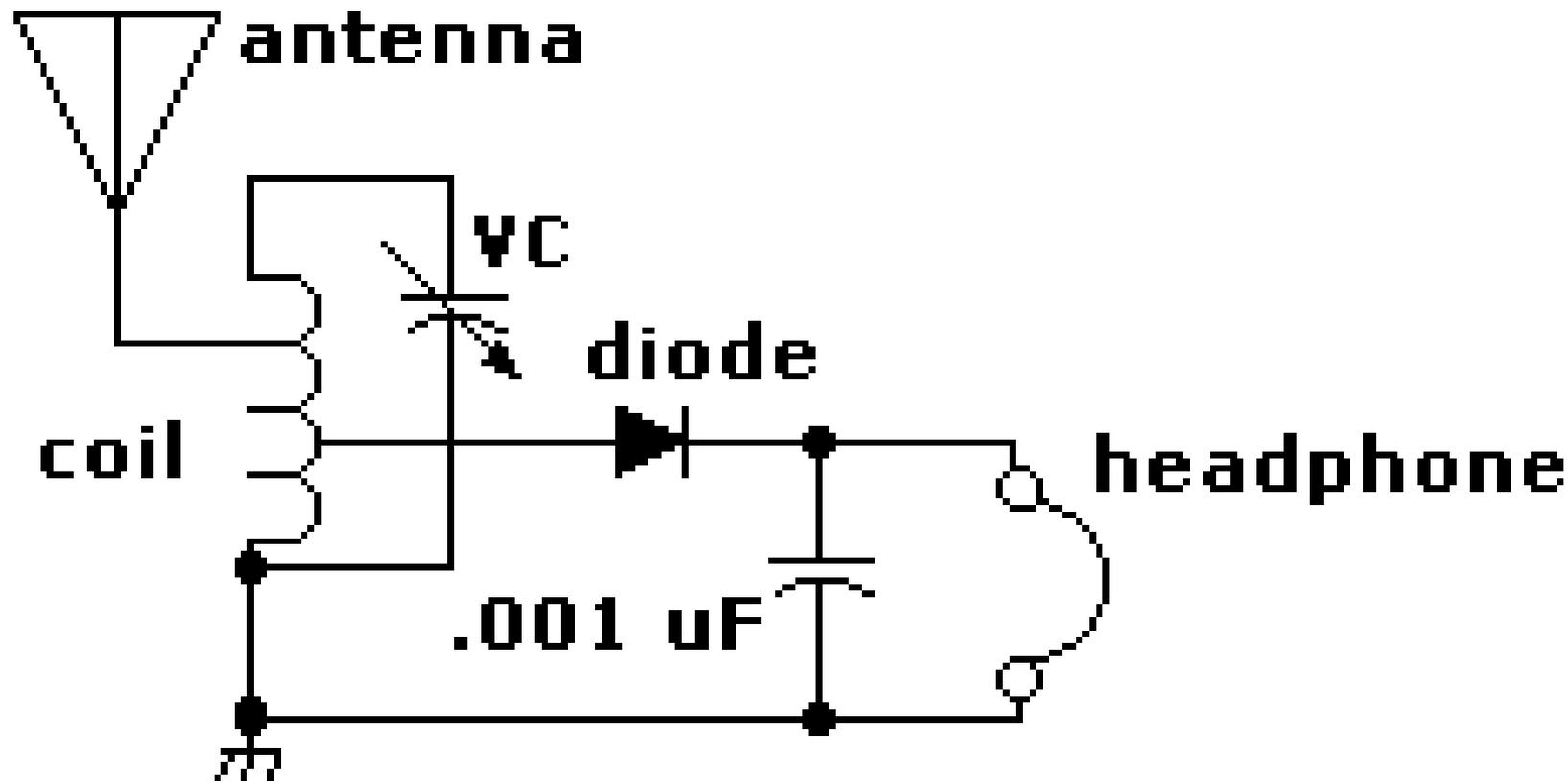


Band Pass Filter

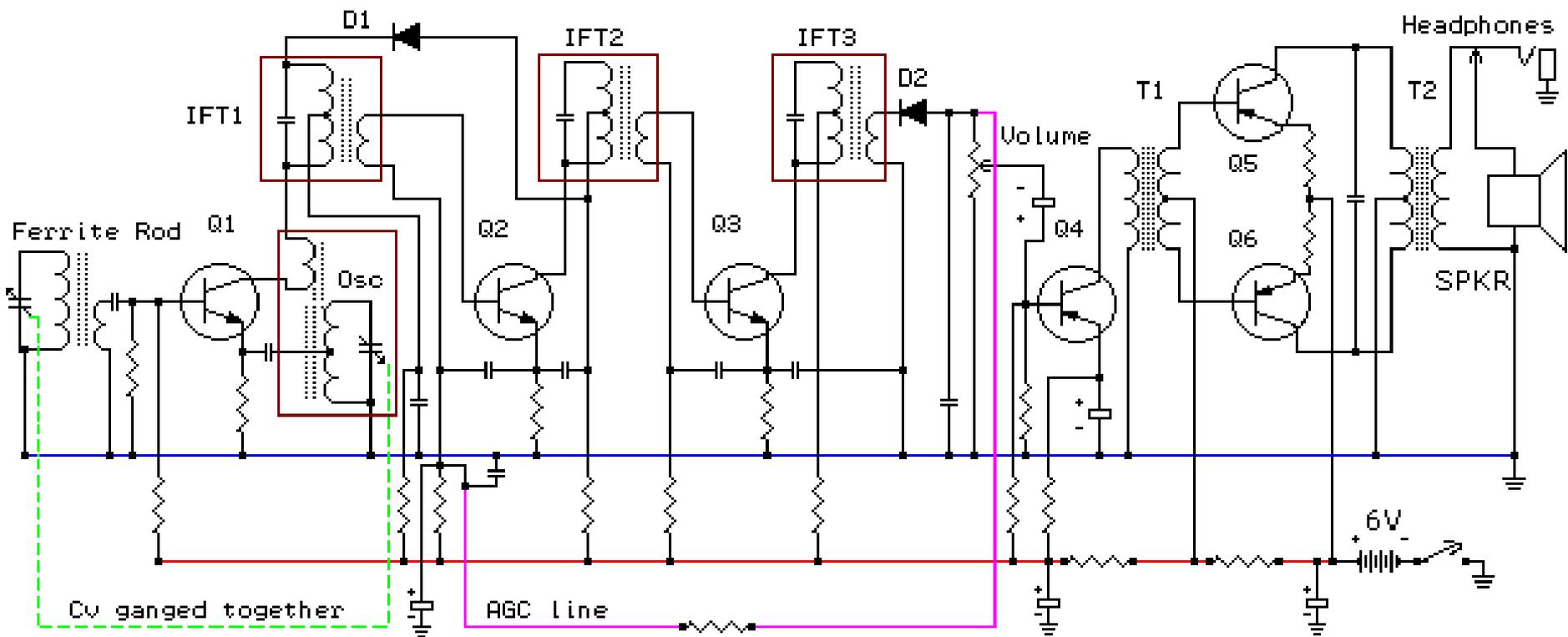


Notch Filter

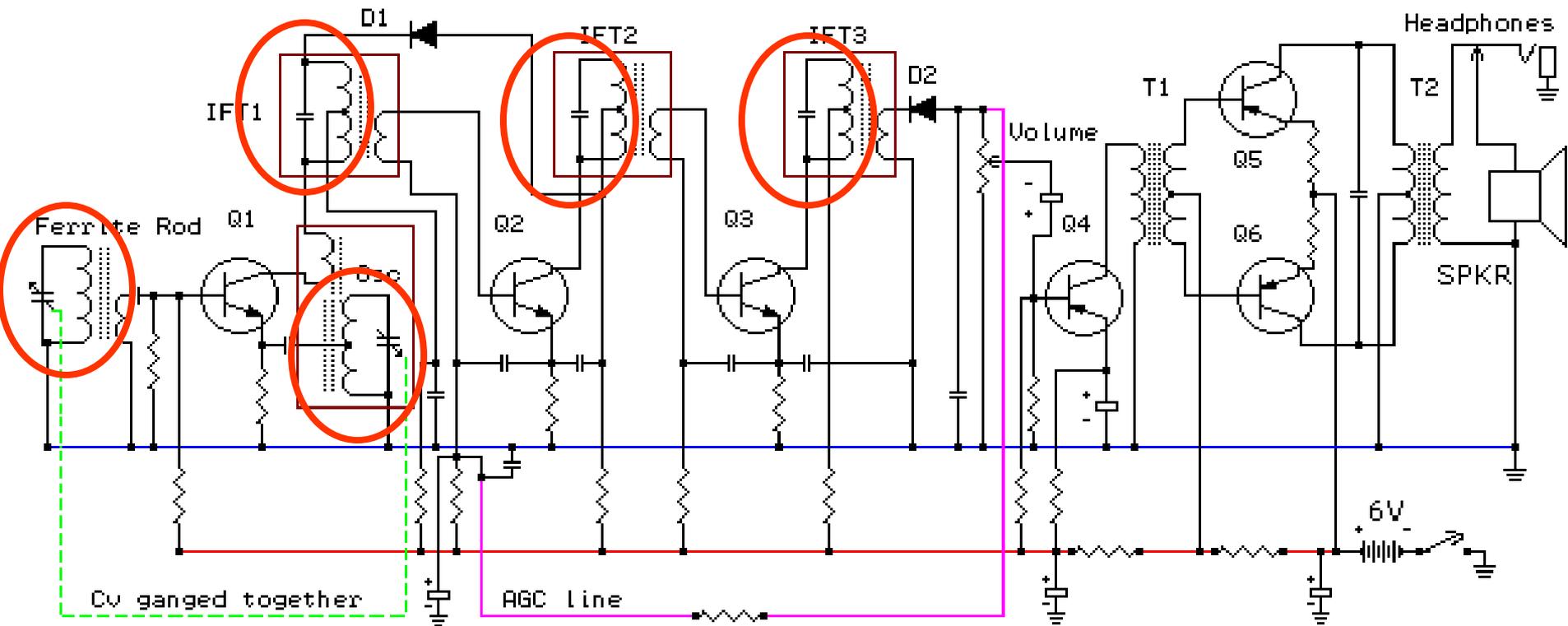
Crystal Radio Tuned Circuit



6 Transistor Radio

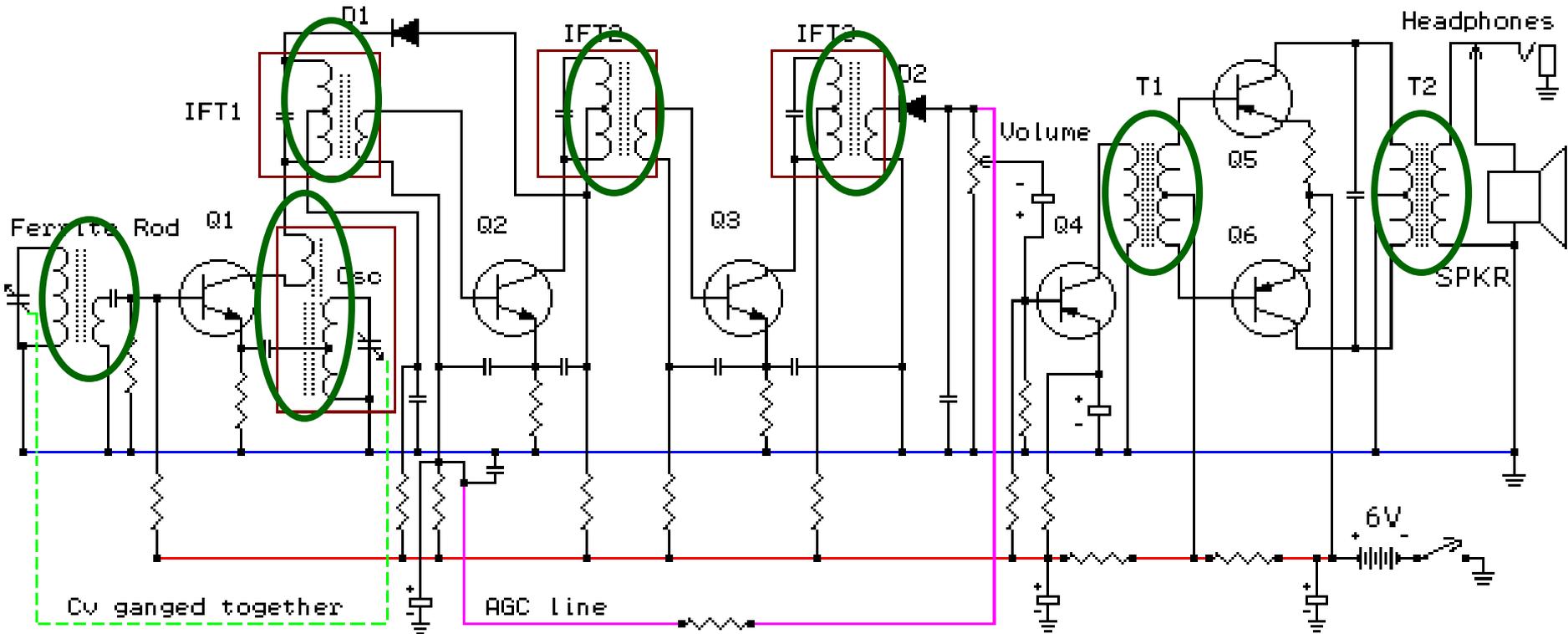


6 Transistor Radio



Tuned Circuits

6 Transistor Radio



Transformers



Questions?